

SCORE: 26 1/2 / 35 POINTS

20 1/2 + 6 GREENSHEET QUIZ SCORE

1. NO CALCULATORS OR NOTES ALLOWED
2. UNLESS STATED OTHERWISE, YOU MUST SIMPLIFY ALL ANSWERS
3. SHOW PROPER CALCULUS LEVEL WORK TO JUSTIFY YOUR ANSWERS

Consider the following statements.

SCORE: 2 / 2 PTS

(i)  $\{x\} \subseteq \{x, y, \{z\}\}$

(ii)  $\{z\} \in \{x, y, \{z\}\}$

(iii)  $\{z\} \subseteq \{x, y, \{z\}\}$

Which of the statements above are true? Circle the correct answer below.

[a] none are true

[b] only (i) is true

[c] only (ii) is true

[d] only (iii) is true

(2) [e] only (i) and (ii) are true

[f] only (i) and (iii) are true

[g] only (ii) and (iii) are true

[h] all are true

Rewrite the following statement using 2 variables and the formal structure mentioned in the 1.1 lecture notes.

SCORE: 0 / 2 PTS

NOTE: Do NOT use any symbols, except for the variables.

"There's an instructor for each class."

There is an instructor  $x$  for a class  $y$

If  $N = \{0, 1, 2, 3, 4, 5, 6, 7, 8\}$  and  $L = \{a, b, c, d, e, f, g, h, i, j, k\}$ ,  
how many elements are in the Cartesian product of  $L$  and  $N$ ?

SCORE: 2 / 2 PTS

9 · 11 = 99 elements

Fill in the blanks for the following formal definitions. Use proper mathematical notation.

SCORE: 2 / 4 PTS

[a] Given sets  $M$  and  $N$ ,  $N$  is a subset of  $M$  (or  $N \subseteq M$ ) if and only if for all  $x \in N$ ,  $x \in M$ .

[b] The Cartesian product of sets  $M$  and  $N$  is  $M \times N =$  the set of all ordered pairs  $(m, n) \in M \times N$

Determine if  $p \oplus q \equiv \sim p \leftrightarrow q$ . State your final answer clearly.

SCORE: 3 / 3 PTS

$p$	$q$	$p \oplus q$	$\sim p$	$\sim p \leftrightarrow q$
T	T	F	F	F
T	F	T	T	T
F	T	T	F	T
F	F	F	T	F

Because  $p \oplus q$  and  $\sim p \leftrightarrow q$  have the same truth values, they are logically equivalent.

1/2

Write the formal definition of a relation used in discrete math. Use correct English and mathematical notation. SCORE: 1/2 / 2 PTS

Given sets A and B, a relation R is a subset of what?  
 $x R y$  IFF  $x$  is related to  $y$  by R and  $(x, y) \in R$ .

Classify each statement as Universal Existential (UE), Existential Universal (EU) or Universal Conditional (UC). SCORE: 1 / 2 POINTS

- [a] All calculus students have passed the same placement test. UE
- [b] Students who have parking stickers can park in lot C. UC (1)

Consider the statement "if  $\frac{1}{x} < 1$ , then  $x > 1$ ". (Assume  $x$  is a particular real number.)  $p \rightarrow q$  SCORE: 3 / 4 POINTS

[a] Write a logically equivalent statement using "is necessary for". Do NOT use statement variables in your final answer.

$x > 1$  is necessary for  $\frac{1}{x} < 1$  (1)

[b] Write a logically equivalent statement using "unless". Do NOT use statement variables in your final answer.

$\frac{1}{x} < 1$  unless  $x \leq 1$

[c] Write the contrapositive of the statement. Do NOT use statement variables in your final answer.

If  $x \leq 1$ , then  $\frac{1}{x} \geq 1$  (1)

[d] Write the negation of the statement. Do NOT use statement variables in your final answer.

$\frac{1}{x} < 1$  and  $x \leq 1$  (1)

Determine if the following argument is valid. State your final answer clearly. SCORE: 7 / 8 PTS  
 NOTES: This is NOT an essay question. Use the method shown in lecture and section 2.3. Do NOT use the Rules of Inference.

If I save a lot of money, then I can quit my second job or I can buy a new car.  
 I did not save a lot of money and I cannot quit my second job.  
 Therefore, I cannot buy a new car.

$P \rightarrow (q \vee r)$   
 $\sim P \wedge \sim q$   
 $\therefore \sim r$   
 (2)

P	q	r	(q ∨ r)	P → (q ∨ r)	~P	~q	~P ∧ ~q	~r
T	T	T	T	T	F	F	F	F
T	T	F	T	T	F	F	F	T
T	F	T	T	T	F	T	F	F
T	F	F	F	F	F	T	F	F
F	T	T	T	T	T	F	F	T
F	T	F	T	T	T	F	F	T
F	F	T	T	T	T	T	T	F
F	F	F	F	F	T	T	T	T

This argument is invalid (1) because there is a critical row where the premises are all true, but the conclusion is false. (2)